

Use Square-Inch Grid Paper or tiles to help you solve these problems. Write a number sentence to go with each problem.

- Roberto made a rectangle with 6 rows and 5 tiles in each row. How many tiles did he use?
- Jackie made a rectangle with 21 tiles. There were 7 tiles in each row. How many rows were there?
- 3. Shannon made a rectangle with 32 tiles. If there were 4 rows, how many tiles were in each row?
- 4. Then Shannon made a different rectangle with her 32 tiles. What other rectangle could Shannon have made?
- 5. A rectangle of 12 tiles has 3 different colors. There is an equal number of tiles of each color. How many tiles of each color are there?

When a rectangle can be made with tiles, the 2 sides of the rectangle are called **factors** of the total number of tiles used. Roberto's rectangle in Question 1 has sides of 6 and 5 tiles so he can write the number sentence  $6\times5=30$ . Roberto's rectangle shows that 5 and 6 are **factors** of 30.

Factors

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- Jackie's rectangle shows that 7 is a factor of 21. Use the number sentence you wrote for Question 2 to name another factor of 21.
- 7. Use your number sentence in Question 3 to name two factors of 32.
- 8. Did you find two more factors in Question 4? What are they?

### **Finding Factors**



Jacob wondered whether he could arrange 24 tiles into 5 rows. He wanted to know if 5 is a factor of 24. He used his calculator to divide 24 into 5 groups.

The factors of a number must be whole numbers that can be multiplied to get the number. For example,  $3\times 8=24$ , so 3 and 8  $^3$  are factors of 24. Three and eight are whole numbers. All the factors of 24 are 1, 2, 3, 4, 6, 8, 12, and 24, because we can multiply pairs of numbers to get 24 in the following ways:  $1\times 24$ ,  $2\times 12$ ,

 $3 \times 8$ , and  $4 \times 6$ .

The factors of a number can also be described as the whole numbers that divide the number evenly. 2 is a factor of 24 because 24  $\div$  2 = 12. But 5 is not a factor of 24 because 24  $\div$  5 = 4.8, and 4.8 is not a whole number.

The number sentence  $24 = 3 \times 8$  tells us

- 24 is a multiple of both 3 and 8.
- 3 and 8 are both factors of 24.

Remember, a **multiple** of a number is the product of that number and another number.

The factors of a number tell us which numbers of rows are possible in rectangles made with that number of tiles. Jacob couldn't make a rectangle with 5 rows and 24 tiles because 6 is not a factor of 24.

- 9. A. Is it possible to make a rectangle with 24 tiles and 6 rows? If so, how many tiles will be in each row? Use your calculator to check.
  - B. Is it possible to make a rectangle with 24 tiles and 7 rows? Use your calculator to check. Explain.

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Factors

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\*Answers and/or discussion are included in the lesson.

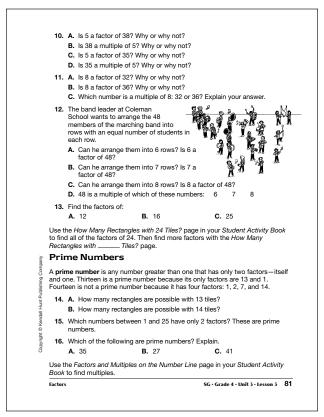
### Student Guide

### Questions 1-16 (SG pp. 79-81)

- **1.**\* 30 tiles;  $6 \times 5 = 30$
- **2.**\*3 rows;  $3 \times 7 = 21$ , or  $21 \div 7 = 3$
- **3.**\* 8 tiles;  $4 \times 8 = 32$
- **4.**\*2 possible rectangles: 2 rows with 16 tiles,  $2 \times 16 = 32$ 1 row with 32 tiles,  $1 \times 32 = 32$
- **5.**\*4 tiles of each color;  $4 \times 3 = 12$
- **6.**  $3; 7 \times 3 = 21$
- **7.** 4 and 8;  $4 \times 8 = 32$
- **8.** Possible factors: 2 and 16;  $2 \times 16 = 32$  or 1 and 32;  $1 \times 32 = 32$
- **9. A.** Yes; 4 tiles in each row;  $24 \div 6 = 4$ 
  - **B.** No;  $24 \div 7 = 3.4285714...$ ; The answer on the calculator is not a whole number.

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- **10. A.** No; Explanations will vary. Using the calculator:  $38 \div 5 = 7.6$ . You cannot make a rectangle with 5 rows and 38 tiles.
  - **B.** No; Explanations will vary. You cannot multiply 5 by a whole number to get 38.
  - **C.** Yes; Explanations will vary. Using the calculator:  $35 \div 5 = 7$ , which is a whole number. You can make a rectangle with 5 rows and 35 tiles. There would be 7 tiles in each row.
  - **D.** Yes,  $5 \times 7 = 35$
- **11. A.** Yes; Explanations will vary.  $32 \div 8 = 4$ . You can make a rectangle with 8 rows and 32 tiles. There will be 4 tiles in each row.
  - **B.** No; Explanations will vary.  $36 \div 8 = 4.5$ . You cannot make a rectangle with 8 rows and 36 tiles.
  - **C.** 32 is a multiple of 8;  $8 \times 4 = 32$
- **12. A.** Yes; Yes;  $48 \div 6 = 8$ ; 8 students in each row
  - **B.** No; No;  $48 \div 7 = 6.8571429...$
  - **C.** Yes; Yes;  $48 \div 8 = 6$ ; 6 students in each row
  - **D.** 6 and 8
- **13. A.** 1, 2, 3, 4, 6, 12
  - **B.** 1, 2, 4, 8, 16
  - **C.** 1, 5, 25
- **14. A.** 1 rectangle: 1 row of 13 tiles.
  - **B.** 2 rectangles: 1 row of 14 tiles and 2 rows of 7 tiles
- **15.** 2, 3, 5, 7, 11, 13, 17, 19, 23
- **16. A.\*** No; Explanations will vary. 35 has more than 2 factors (1, 5, 7, 35)
  - **B.\*** No; Explanations will vary. 27 has more than 2 factors (1, 3, 9, 27)
  - **C.\*** Yes; Explanations will vary. Systematic testing for factors by division shows that 41 has only 2 factors (1 and 41).



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<sup>\*</sup>Answers and/or discussion are included in the lesson.

### More Tile Problems

Use Square-Inch Grid Paper to help you solve these problems. Write a number sentence to go with each problem.

- 1. Irma made a rectangle with 28 tiles. If there were 7 rows, how many tiles were in each row?
- 2. Keenya made a rectangle with 8 rows and 5 tiles in each row. How many tiles did she use?
- Michael made a rectangle with the same number of tiles as Keenya's but with a different number of rows. Describe the rectangle that Michael could have made.
- 4. Find another rectangle that Michael could have made.
- 5. Romesh made a rectangle with 42 tiles. There were 6 tiles in each row. How many rows were there?
- 6. A rectangle of 18 tiles has 3 different colors. There is an equal number of tiles of each color. How many tiles of each color are there? How do you know? Draw a picture to show your solution.

### **More Finding** Factors Problems

7. A. Make a table like this one to show all the rectangles that can be made with 28 tiles. You can use a calculator. multiplication facts, or Square-Inch Grid Paper to help you divide.

Rectangles with 28 Tiles					
Number of Rows	Division Sentence				
1	28	28 ÷ 1 = 28			
2	14	28 ÷ 2 = 14			
	~				

- B. Use the table to help you list the factors of 28.
- 8. A. Make a table similar to that in Question 7 to show all the rectangles that can be made with 48 tiles
  - B. List the factors of 48.

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### Homework (SG pp. 82-83)

### Questions 1-15

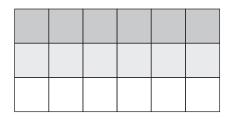
- **1.** 4 tiles;  $28 \div 7 = 4$
- **2.** 40 tiles;  $8 \times 5 = 40$
- **3–4.** 3 possible rectangles

1 row with 40 tiles,  $1 \times 40 = 40$ 

2 rows with 20 tiles,  $2 \times 20 = 40$ 

4 rows with 10 tiles,  $4 \times 10 = 40$ 

- **5.** 7 rows;  $42 \div 6 = 7$
- **6.** 6 tiles of each color;  $18 \div 3 = 6$



### 7. A. Rectangles with 28 Tiles

Number of Rows	Number in Each Row	Division Sentence
1	28	28 ÷ 1 = 28
2	14	28 ÷ 2 = 14
4	7	28 ÷ 4 = 7
7	4	28 ÷ 7 = 4
14	2	28 ÷ 14 = 2
28	1	28 ÷ 28 = 1

**B.** 1, 2, 4, 7, 14, 28

# Rectangles with 48 Tiles

Number of Rows	Number in Each Row	Division Sentence
1	48	48 ÷ 1 = 48
2	24	48 ÷ 2 = 24
3	16	48 ÷ 3 = 16
4	12	48 ÷ 4 = 12
6	8	48 ÷ 6 = 8
8	6	48 ÷ 8 = 6
12	4	48 ÷ 12 = 4
16	3	48 ÷ 16 = 3
24	2	48 ÷ 24 = 2
48	1	48 ÷ 48 = 1

**B.** 1, 2, 3, 4, 6, 8, 12, 16, 24, 48

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- **9. A.** Yes; Explanations will vary.  $3 \times 9 = 27$ ; If you skip count by 3s you hit 27. You can make a rectangle with 3 rows and 27 tiles. 9 tiles would be in each row.
  - **B.** No; Explanations will vary.  $32 \div 7 = 4.5714...$ ; You cannot make a rectangle with 7 rows and 32 tiles.
- **10.** Possible response: 8, 12, 16, 20, 24
- **11. A.** Yes; Explanations will vary.  $7 \times 5 = 35$ 
  - **B.** No; Explanations will vary.  $42 \div 8 = 5.25$ , 8 is not a factor of 42.
- **12. A.** 1, 2, 3, 6
  - **B.** 1, 3, 5, 15
  - **C.** 1, 5, 25
  - **D.** 1, 2, 13, 26
- **13. A.** No; Explanations will vary. 39 has four factors: 1, 3, 13, and 39. You can make more than one rectangle with 39 tiles.
  - **B.** No; Explanations will vary. 51 has four factors: 1, 3, 17, and 51. You can make more than one rectangle with 51 tiles.
  - **C.** Yes; Explanations will vary. A systematic check for factors shows that 67 has only 1 and itself as factors. (See Content Note in Lesson Guide 2 for a discussion of testing whether a number is prime.)
- **14.** 29, 31, 37, 41, 43, and 47. Solution strategies will vary.
- - **A.** Numbers that have 6 as a factor are 6, 12, 18, 24, and 30.
  - **B.** Numbers that have 3 as a factor are 3, 6, 9, 12, 15, 18, 21, 24, 27, 30.
  - **C.** Possible responses: Every number that has 6 as a factor also has 3 as a factor, but not vice versa.

9. A. Is 3 a factor of 27? How do you know?
B. Is 7 a factor of 32? How do you know?
10. List 5 multiples of 4.
11. A. Is 35 a multiple of 7? How do you know?
B. Is 42 a multiple of 8? How do you know?
12. List all the factors of:
A. 6
B. 15
C. 25
D. 26
13. Which of the following are prime numbers? How do you know?
A. 39
B. 51
C. 67
14. Challenge question: Find all the prime numbers between 25 and 50. Explain what you did to find your answer.
15. A. Draw a number line like the one below. Mark the numbers that have 6 as a factor on this number line.
B. With a pencil of a different color, mark the numbers that have 3 as a factor.
C. Compare the multiples. What do you notice?

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use squa		our classroom to fill in t ou. The first two lines a	
Number of Rows	Number in Each Row	Division Sentence	Factors
1	24	24 ÷ 1 = 24	1, 24
2	12	24 ÷ 2 = 12	2, 12
2. Is 24 a m	ultiple of 5? How do	you know?	
3. Is 3 a fac	. Is 3 a factor of 24? How do you know?		
<b>1.</b> Is 24 a m	ultiple of 9? How do	you know?	
	e factors of 24.		

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<u> </u>		y use square-inch tiles	to help you.
Number of Rows	Number in Each Row	Division Sentence	Factors
2. List all th	e factors of your num	ber.	
3 Is your ni	umber a multiple of 87	? How do you know?	

### **Student Activity Book**

# How Many Rectangles with 24 Tiles? Questions 1–5 (SAB p. 41)

**1.\*** How Many Rectangles with 24 Tiles?

Number of Rows	Number in Each Row	Division Sentence	Factors
1	24	24 ÷ 1 = 24	1, 24
2	12	24 ÷ 2 = 12	2, 12
3	8	24 ÷ 3 = 8	3, 8
4	6	24 ÷ 4 = 6	4, 6
6	4	24 ÷ 6 = 4	6, 4
8	3	24 ÷ 8 = 3	8, 3
12	2	24 ÷ 12 = 2	12, 2
24	1	24 ÷ 24 = 1	24, 1

Explanations will vary for 2–4. One possible response is given for each.

- 2. No. You do not hit 24 if you skip count by 5s.
- **3.** Yes. You can make a rectangle with 3 rows and 24 tiles. There will be 8 tiles in each row.
- **4.** No.  $24 \div 9 = 2.666 \dots$
- **5.** 1, 2, 3, 4, 6, 8, 12, 24

# How Many Rectangles with \_\_\_\_\_ Tiles? Questions 1–4 (SAB p. 42)

**1–4.** Responses will vary depending on number given by the teacher.

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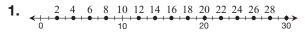
<sup>\*</sup>Answers and/or discussion are included in the lesson.

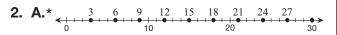
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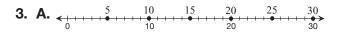
# Factors and Multiples on the Number Line (SAB p. 43)

### Questions 1-3





**B.\*** All of them. They are divisible by 3.



**B.** Yes, they are all divisible by 5.

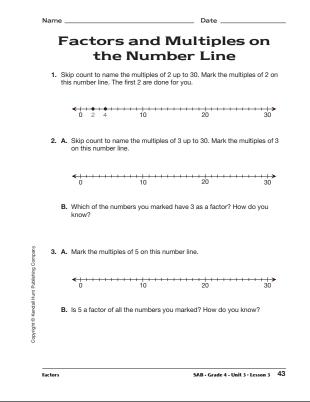
# How Many Rectangles with 30 Tiles? Questions 1–5 (SAB p. 45)

1. How Many Rectangles with 30 Tiles?

Number of Rows	Number in Each Row	Division Sentence	Factors
1	30	30 ÷ 1 = 30	1, 30
2	15	30 ÷ 2 = 15	2, 15
3	10	30 ÷ 3 = 10	3, 10
5	6	30 ÷ 5 = 6	5, 6
6	5	30 ÷ 6 = 5	6, 5
10	3	30 ÷ 10 = 3	10, 3
15	2	30 ÷ 15 = 2	15, 2
30	1	30 ÷ 30 = 1	30, 1

Explanations will vary for 2–4. One possible response is given for each.

- **2.** Yes. You can make a rectangle with 2 rows and 30 tiles
- **3.** Yes. You hit 30 if you skip count by 3.
- **4.** No.  $30 \div 4 = 7.5$ , not a whole number.
- **5.** 1, 2, 3, 5, 6, 10, 15, 30



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	110	with	y Recta 30 Tiles	Signes
		table and list all the	rectangles possible wit The first line is done for	
	Number of Rows	Number in Each Row	Division Sentence	Factors
	1	30	30 ÷ 1 = 30	1, 30
ompany				
Dilshing C	2. Is 30 a m	ultiple of 2? How do	you know?	
III Hunt Pu	3. Is 3 a fac	tor of 30? How do y	ou know?	
Copyright © Kendall Hunt Publishing Company	4. Is 30 a m	ultiple of 4? How do	you know?	
Copyrigh	5. List all the	e factors of 30.		

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<sup>\*</sup>Answers and/or discussion are included in the lesson.

Teacher Guide

# **Teacher Guide**

# How Many Rectangles with 20 Tiles? Questions 1–4 (TG)

**1.** How Many Rectangles with 20 Tiles?

Number of Rows	Number in Each Row	Division Sentence	Factors
1	20	20 ÷ 1 = 20	1, 20
2	10	20 ÷ 2 = 10	2, 10
4	5	20 ÷ 4 = 5	4, 5
10	2	20 ÷ 10 = 2	10, 2
20	1	20 ÷ 20 = 1	20, 1

**2.** 1, 2, 4, 5, 10, 20

Explanations will vary for 3–4. One possible response is given for each.

- **3.** Yes. You can divide 2 into 20 evenly.
- **4.** No. You do not hit 20 if you skip count by 6.

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<sup>\*</sup>Answers and/or discussion are included in the lesson.